

V. Location $\leftarrow$ find the data value

eg I want to know 75th of the score for this class.

steps: 1. Sort the data values

2. Compute the location L , where

$$L = \% \cdot n$$

$\leftarrow L = \text{percentile} \cdot \text{total}$

eg $L = 0.75 \cdot 34$

A. If L is an integer, then count it.

B. If L is a decimal, then $\frac{L^{\text{th}} \text{ value} + (L+1)^{\text{th}} \text{ value}}{2}$

$\rightarrow L = 7.8$,

data = $\frac{7^{\text{th}} \text{ value} + 8^{\text{th}} \text{ value}}{2} = "86"$

eg 1, 3, 5, 7, 10

If $L = 2$, data = $\boxed{3}$ $\leftarrow$ data value

If $L = 3$, data = $\boxed{5}$

If $L = 5$, data = $\boxed{10}$

If $L = 1.7$, data = $\frac{1^{\text{st}} \text{ data} + 2^{\text{nd}} \text{ data}}{2} = \frac{1 + 3}{2} = \boxed{2}$

If $L = 3.3$, data = $\frac{3^{\text{rd}} \text{ data} + 4^{\text{th}} \text{ data}}{2} = \frac{5 + 7}{2} = \boxed{6}$

eg 4, 6, 10, 15

If $L = 1$, data = $\boxed{4}$

If $L = 3$, data = $\boxed{10}$

If $L = 2.7$, data = $\frac{2^{\text{nd}} \text{ data} + 3^{\text{rd}} \text{ data}}{2} = \frac{6 + 10}{2} = \boxed{8}$

If $L = 3.9$, data = $\frac{3^{\text{rd}} \text{ data} + 4^{\text{th}} \text{ data}}{2} = \frac{10 + 15}{2} = \boxed{12.5}$

eg 1, 2, 3, 5, 7, 9, 10

If $L = 6.4$, data = $\frac{6^{\text{th}} \text{ data} + 7^{\text{th}} \text{ data}}{2} = \frac{9 + 10}{2} = \boxed{9.5}$

If $L = 5$, data = $\boxed{7}$

Eg Find the data value of the 18th percentile.

19	19	20	20	20	20	22	22	22	22
23	23	23	23	23	23	23	24	24	24
24	24	25	25	25	25	25	25	25	26
26	26	26	26	26	27	27	28	28	30

S: $n = 40$, $18\% = 0.18$ ← to sort

$$L = 0.18 \cdot 40 = 7.2$$

$$P_{18} = \frac{7^{\text{th}} \text{ data} + 8^{\text{th}} \text{ data}}{2}$$
$$= \frac{22 + 22}{2}$$

← keep it simple

$$= \boxed{22}^2 \text{ chips}$$

Eg Find the data value of the 75th percentile.

19	19	20	20	20	20	22	22	22	22
23	23	23	23	23	23	23	24	24	24
24	24	25	25	25	25	25	25	25	26
26	26	26	26	26	27	27	28	28	30

10th
↓

← 30th

S: $L = 0.75 \cdot 40 = 30$

$$P_{75} = \boxed{26} \text{ chips}$$

Eg Find the data value of the 48th percentile.

19	19	20	20	20	20	22	22	22	22
23	23	23	23	23	23	23	24	24	24
24	24	25	25	25	25	25	25	25	26
26	26	26	26	26	27	27	28	28	30

19th 20th

S: $L = 0.48 \cdot 40 = 19.2$

$$\text{Data} = \frac{24 + 24}{2}$$

$$= \boxed{24} \text{ chips}$$

Eg. Given the sorted list of 20 values:

3 5 6 7 8 9 11 12 14 18 20 24 26
27 28 30 32 34 35 40

8th

Eg. Given the sorted list of 20 values:

3 5 6 7 8 9 11 12 14 18 20 24 26
27 28 30 33 34 35 40.

Find the value of P_{40} .

S: $L = 0.4 \cdot 20 = 8$

$$P_{40} = \boxed{12}$$

Eg. Given the sorted list of 20 values:

3 5 6 7 8 9 11 12 14 18 20 24 26
27 28 30 33 34 35 40.

Find the value of P_{47} .

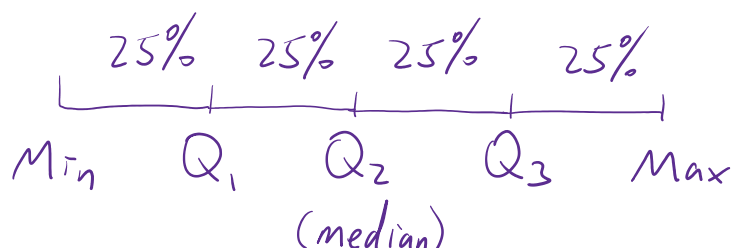
S: $L = 0.47 \cdot 20 = 9.4$

$$P_{47} = \frac{14 + 18}{2} = \boxed{16}$$

9 9.4 10
↓

iii. Quartile $\leftarrow 25^{th}$

It is a special measure of position for the n number data value. It divides into 4 interval



Min Q_1 Q_2 Q_3 Max
(median)

We have the 5-number summary:

They are as following: Minimum, first quartile Q_1 , second quartile Q_2 (median), third quartile Q_3 and Maximum

Eg Find the 5-number summary for the following:

19	19	20	20	20	20	22	22	22	22	^{10th}
23	23	23	23	23	23	23	24	24	24	✓
24	24	25	25	25	25	25	25	25	26	
26	26	26	26	26	27	27	28	28	30	← 40

S: min = 19 ✓, max = 30 ✓

$$L_{25} = 0.25 \cdot 40 = 10$$

$$Q_1 = \boxed{22}$$

$$L_{50} = 0.5 \cdot 40 = 20$$

$$Q_2 = \boxed{24}$$

$$L_{75} = 0.75 \cdot 40 = 30$$

$$Q_3 = \boxed{26}$$

The 5-number summary: 19, 22, 24, 26, 30

Eg Find the 5-number summary for the following datas:

32	27	26	20	17	39	41	23	24	27
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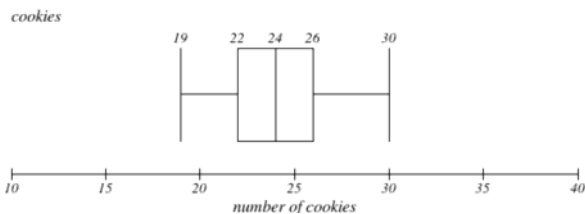
S: Stat → 1: Edit → CALC → 1: 1-Var Stats

VI. Boxplot

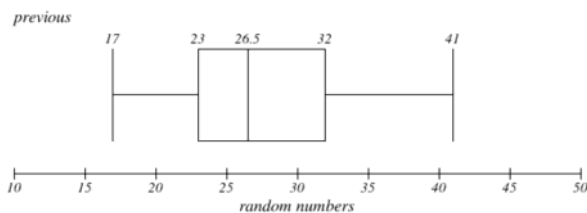
It gives a series of distribution, which it displays the distribution for a 5-number summary

<https://www.imathas.com/stattools/boxplot.html>

or: TI-84 ← highly recommend

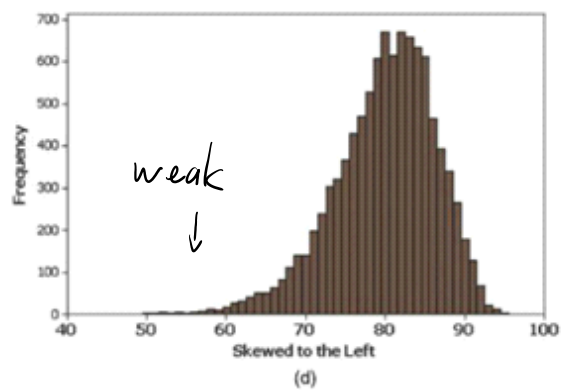
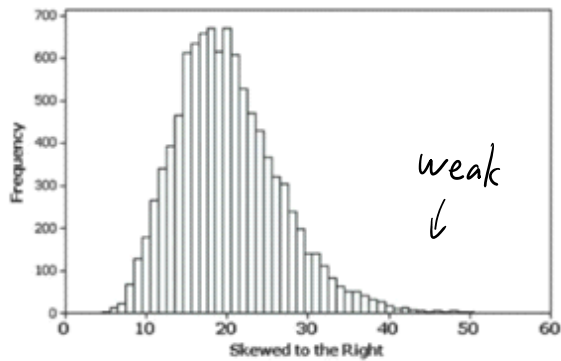
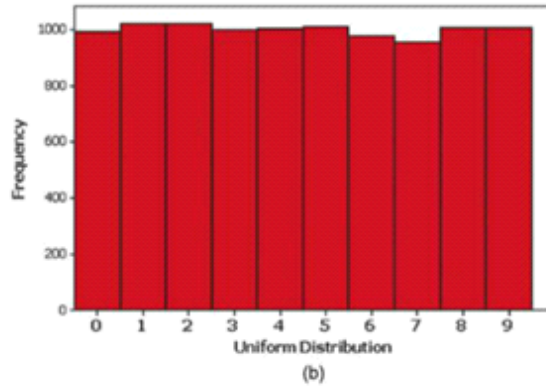
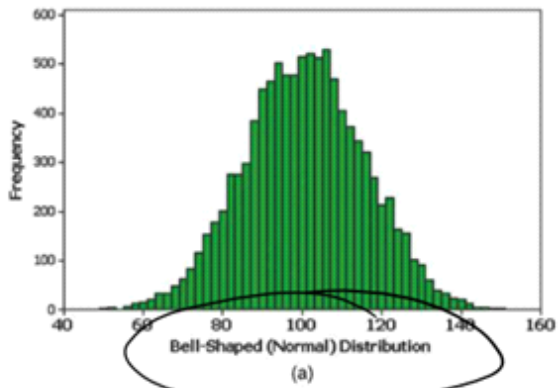


eg



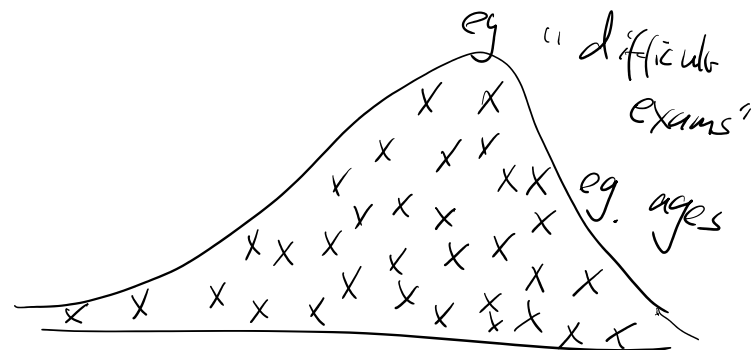
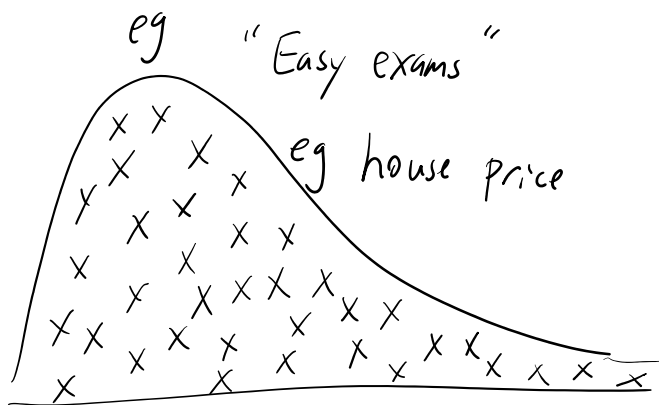
TI-84: statplot → on → graph → Zoom → 9: ZoomStat

eg. Discuss the Shape



right-skew (skew to the right)

left-skew (skew to the left)



X's are random variables